MOHAWK VALLEY COMMUNITY COLLEGE

COURSE OUTLINE

MA 125

COLLEGE ALGEBRA AND TRIGONOMETRY

 Prepared by: September 2004

 Reviewed and Found Acceptable – 5/05

 Reviewed and Found Acceptable – 5/06

Reviewed and Revised – 5/07

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Reviewed and Revised – 4/17

Reviewed and Revised – 6/18

Course Outline

Title: College Algebra and Trigonometry

Catalog Number: MA 125

Credit Hours: 4

Lab Hours: 0

Prerequisite: An appropriate high school GPA, or placement test score , or MA115 Intermediate Mathematics, or completion of one college-

 level math course.

Catalog Description: This course prepares students for MA150 Precalculus. Topics include linear and quadratic equations; inequalities; rational expressions; trigonometric functions; graphs of linear, quadratic, piecewise, and trigonometric functions; and, systems of equations. Algebraic and trigonometric manipulations, and problem-solving are emphasized.

COURSE TEACHING GOALS FOR ALL TOPICS:

GOAL A: Use mathematical processes to acquire and convey knowledge.

GOAL B: Systematically solve problems.

GOAL C:  Demonstrate an awareness of the historical development of algebra and trigonometry and how they relate to various disciplines.

**SUNY Learning Outcomes**

1. The student will develop well reasoned arguments.
2. The student will identify, analyze, and evaluate arguments as they occur in their own and other’s work.
3. The student will demonstrate the ability to interpret and draw inferences from mathematical models such as formulas, graphs, tables, and schematics.
4. The student will demonstrate the ability to represent mathematical information symbolically, visually, numerically, and verbally.
5. The student will demonstrate the ability to employ quantitative methods such as arithmetic, algebra, geometry, or statistics to solve problems.
6. The student will demonstrate the ability to estimate and check mathematical results for reasonableness.

TOPIC 1: Fundamental Concepts and Algebraic Operations

 Basic algebraic definitions and operations are developed. Manipulations in order

 to simplify algebraic expressions are studied.

Student Outcomes:

The student will:

1.1 Identify characteristics and ordering of subsets of the real numbers

1.2 Demonstrate an understanding of the properties of addition and multiplication of algebraic expressions

1.3 Simplify algebraic expressions by removing parentheses

1.4 Simplify or evaluate algebraic expressions using the order of operations agreement

1.5 Perform basic operations (addition, subtraction, multiplication, and division) on polynomials

1.6 Provide solutions to problems involving exponents or roots

1.7 Perform operations on exponential expressions

1.8 Perform operations on expressions involving radicals

1.9 Simplify expressions involving exponents or radicals

1.10 Change from radical form to rational exponent form, and vice-versa

1.11 Change from logarithmic expressions into exponential and vice-versa

TOPIC 2: Functions and Graphs

 After the basic algebraic techniques are established, an introduction to the concept of, properties of, graphs of, and operations with functions are developed and studied.

Student Outcomes:

The student will:

2.1 Evaluate functions

2.2 Write functions from a given statement

2.3 Sketch the graph of a function by plotting points

2.4 Sketch the graph of piecewise-defined functions

2.5 Put the equation of a circle in standard form by completing the square

2.6 Determine whether a given expression represents a function

2.7 Determine the domain and range of a function, both algebraically and graphically

2.8 Use symmetry, translations, and reflections as aids in graphing functions

2.9 Add, subtract, multiply and divide functions

2.10 Form the composition of two functions

2.11 Determine if a function is one-to-one

2.12 Find the inverse function of a given one-to-one function

2.13 Given two functions, determine if one function is the inverse of the other

2.14 Given a graph (or equation) obtained from transformations of a basic function,

 write the equation (or draw the graph) of the transformed function

2.15 Determine the vertex of a quadratic function by completing the square

2.16 Use linear models to analyze a quantitative relationship

2.17 Use quadratic models to analyze a quantitative relationship

TOPIC 3: Operations with Algebraic Expressions

 Special products and factoring are developed. Additionally, the

 manipulation of algebraic fractions is studied.

Student Outcomes:

The student will:

3.1 Factor trinomials over the rational numbers

3.2 Factor common factors and factor by grouping

3.3 Factor the difference of two squares and the sum or difference of two cubes

3.4 Perform operations (reducing, addition, subtraction, multiplication, division) on

 rational expressions

3.5 Simplify complex fractions

3.6 Solve equations involving fractions which lead to linear and quadratic equations, including those having extraneous solutions

TOPIC 4: Solutions of Equations and Inequalities

Solutions of linear and fractional equations are studied. The quadratic equation is solved by factoring, completing the square and by use of the quadratic formula. Algebraic solution of inequalities and inequalities involving absolute values complete this portion.

Student Outcomes:

The student will:

4.1 Solve linear equations in one unknown

4.2 Solve applied work problems (including applications which use formulas) that yield a linear equation with one unknown.

4.3 Solve quadratic equations having real or complex roots

4.4 Solve absolute values and inequalities

4.5 Solve quadratic inequalities

4.6 Solve rational inequalities

4.7 Solve exponential and logarithmic equations leading to linear equations

4.8 solve applied problems involving pH

TOPIC 5: Systems of Equations

 Systems of linear equations are solved using graphical, algebraic and

 matrix methods.

Student Outcomes:

The student will:

5.1 Graph linear equations in two variables

5.2 Solve systems of two linear equations in two unknowns algebraically (by substitution and also by elimination)

5.3 Solve systems of linear equations with three unknowns algebraically

5.4 Determine whether a system of linear equations is consistent, dependent, or inconsistent, and discuss what this means algebraically and geometrically

5.5 Solve a non-linear system of equations algebraically

TOPIC 6: Introduction to Trigonometry

 This portion of the course assumes no prior study of trigonometry and is taught as a first course for the student on this subject. Angle measure

 (using both degree and radians) is developed. Right triangle trigonometry

 is first developed, followed by the development of the general

 trigonometric functions through the use of the unit circle.

Student Outcomes:

The student will:

6.1 Determine the values of the trigonometric functions in exact form for multiples of

 π/2, π, π/4, π/3, and π/6

6.2 Convert the measure of an angle from degrees to radians, and vice-versa, by

 using a calculator, and also exactly

6.3 Determine any number of angles that are coterminal with a given angle

6.4 Use the definitions of the trigonometric functions to find the value of a trigonometric function of an angle

6.5 Determine the sign of a trigonometric function of an angle

6.6 Use the reference angle to find the values of trigonometric functions of any angle

6.7 Determine the angle(s), given the value of a trigonometric function of an angle

6.8 Use proper notation for inverse trigonometric functions

TOPIC 7: Applications of Trigonometry

 Use of the calculator to find the trigonometric values is taught. The

 method of finding the trigonometric values of special angles (30º, 45º, 60º

 and the quadrantal angles) is shown. Applications of right triangle

 trigonometry are studied.

Student Outcomes:

The student will:

7.1 Use right triangle trigonometry to find unknown parts of a right triangle

7.2 Solve applied problems involving right triangles

TOPIC 8: More Topics in Trigonometry

Graphing the sine and cosine functions is studied. Oblique triangles with the Law of Sines and the Law of Cosines are studied.

Student Outcomes:

The student will:

8.1 Sketch the graphs of *y = sin (x )* and *y = cos (x)*

8.2 Solve oblique triangles using the law of sines

* 1. Solve oblique triangles using the law of cosines

Teaching Guide

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Credit Hours: 4

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